

## Experimental Competition - Problem No. 2

### Black box

#### APPARATUS AND MATERIALS

1. A double beam oscilloscope.
2. A function generator capable to generate sine, triangle and square waves over the 0.02 Hz to 2 MHz range.
3. A "Black box" with two groups of connectors: the ABCD group and A'B'C'D' group.  
 Besides, there are also two connectors for the standard resistor  $R_n = 5 \text{ k}\Omega$ , which is isolated from the two groups.
4. Conductors of negligible resistance.
5. Graph paper.

*Warning:* You are not allowed to open the black box.

#### EXPERIMENT

In the black box, there are two groups of passive elements (that are elements of the types: resistor  $R$ , capacitor  $C$  or inductor (induction coil)  $L$ ). The first group consists of three elements  $Z_1, Z_2, Z_3$  connected in a star circuit as shown in Figure 1. The elements are led out to the connectors A, B, C and D, with A - the common connector of the ABCD group. The second group consists of three elements  $Z'_1, Z'_2, Z'_3$  connected in the same manner to connectors A', B', C' and D', with A'- the common connector of the A'B'C'D' group (see Figure 2).

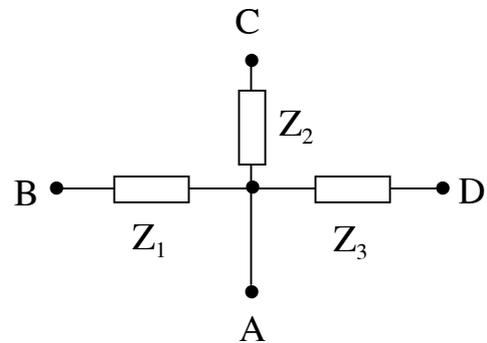


Figure 1

1. By using the oscilloscope and the function generator, determine the type and the parameter (that is resistance of  $R$ , capacity of  $C$ , inductivity of  $L$ ) of each of the elements  $Z_1, Z_2, Z_3$  and  $Z'_1, Z'_2, Z'_3$ . **[5.0 pts]**

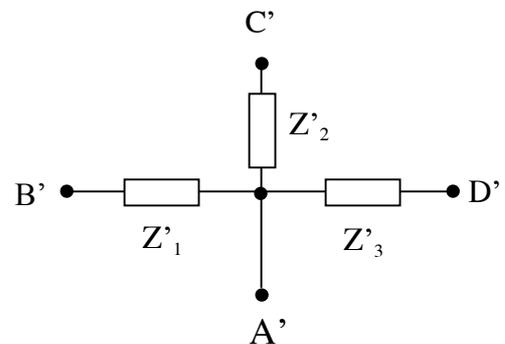


Figure 2

2. Connect five points B, C, B', C' and D' together. We obtain a new black box with terminals DD'A' (called DD'A').
  - a. Draw the electric circuit of this black box.
  - b. Apply a sine wave from the generator to connectors D and A'.

Plot a graph of the ratio of the voltage amplitudes  $K = \frac{U_{D'A'}}{U_{DA'}}$  and the phase shift  $\varphi$

between these voltages as functions of the frequency  $f$  of the signal.

- c. The graphs possess a particular point at a certain frequency  $f_0$ . Determine the value of the frequency  $f_0$ , the ratio  $K = \frac{U_{D'A'}}{U_{DA'}}$  and the phase shift  $\varphi$  at this frequency.

- d. Derive the relation between  $f_0$  and the parameters of the elements in the black box and calculate the values of  $f_0$ . **[5.0 pts]**